

# Crystal structure of mixed fluorites $Ca_{1-x}Sr_xF_2$ and $Sr_{1-x}Ba_xF_2$ and luminescence of $Eu^{2+}$ in this crystals.

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**Abstract.** Within the framework of the virtual crystal method implemented in the shell model and pair potential approximation the crystal structure of mixed fluorites  $Ca_{1-x}Sr_xF_2$  and  $Sr_{1-x}Ba_xF_2$  has been calculated. The structure of impurity center  $Eu^{2+}$  and the distance  $E^{2+} - F^-$  in this crystals have been also calculated. The low level position of excited  $4f^65d$  configuration of the  $Eu^{2+}$  ion has been expressed using phenomenological dependence on distance  $Eu^{2+} - F^-$ . The dependences of Stokes shift and Huang-Rhys factor on  $x$  have been received for yellow luminescence in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$ . The value  $x$ , for which the  $e_g$ -level of  $Eu^{2+}$  ion will be in conduction band in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$  has been calculated.

## 1 Introduction

Fluorites  $CaF_2$ ,  $SrF_2$ ,  $BaF_2$  and mixed crystals on their base attract attention of researchers more than four decades [1, 2, 3, 4, 5]. The crystals, doped by rare-earth ions, are good luminophors and are a basis for solid state lasers. The properties of luminescence and absorption depend on electronic structure of matrix crystal. The blue luminescence with zero phonon line (ZPL) is observed in  $Ca_{1-x}Sr_xF_2 : Eu^{2+}$ . The yellow luminescence without ZPL is observed in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$  at  $x > 0,2$ .

## 2 Calculation of the crystal structure

### $Ca_{1-x}Sr_xF_2$ and $Sr_{1-x}Ba_xF_2$ .

The method of virtual crystal have been implemented within the framework of the pair potential approximation and shell model. The method used has been described in previous work [6] . We have calculated the crystal structure of mixed fluorites  $Ca_{1-x}Sr_xF_2$  and  $Sr_{1-x}Ba_xF_2$  and of impurity center  $Eu^{2+}$  in this crystals. Dependence of a lattice constant of  $Sr_{1-x}Ba_xF_2$  from  $x$  is given on fig.1.

The calculated dependence is in agreement with Vegard rule, though at medial concentrations is appreciable some difference from results of calculation. Similar dependence has been calculated for  $Ca_{1-x}Sr_xF_2$ .

## 3 Impurity ion $Eu^{2+}$ in crystals $Ca_{1-x}Sr_xF_2$ and $Sr_{1-x}Ba_xF_2$

The luminescence and adsorption spectra of  $Eu^{2+}$  in  $Ca_{1-x}Sr_xF_2$  ,  $Sr_{1-x}Ba_xF_2$  deals with interconfigurational transitions between low excited levels of  $4f^65d$  configuration and by  $^8S(4f^7)$  ground state [5]. The ion  $Eu^{2+}$  is in center of cube formed by eight fluorines  $F^-$ . The splitting of  $^8S(4f^7)$  ground state is small in cubic crystal field and does not exceed  $0,2cm^{-1}$  [7]. Level  $5d$  is enough feebly bound by with  $4f^6$  orbitals in excited configuration  $4f^65d$ . The level splits to  $e_g$  and  $t_{2g}$  levels  $12 - 16 \times 10^3cm^{-1}$  [5]. The split considerably exceeds  $LS$  interaction in  $t_{2g}$  state and multiplet split of  $4f^6$  levels [8]. Spectrum of the impurity ion is substantially defined by distance impurity ion–ligand. We have calculated the distance  $Eu^{2+} - F^-$  in the crystals and then have calculated a phenomenological dependence of standing  $e_g$  and  $t_{2g}$  levels from the distance. Standing of  $e_g$  level in  $Ca_{1-x}Sr_xF_2 : Eu^{2+}$ , is expressed by dependence:

$$\nu(r) = C + \frac{A}{r^n} - \frac{B}{r^k} \quad (1)$$

where  $n = 12$ ,  $k = 5$ . The first term determines standing of  $5d$  level in free ion  $Eu^{2+}$ , the second term determines shift of the level at placing  $Eu^{2+}$  in a crystal and third term deals with influence of crystal field on  $t_{2g} - e_g$  splitting. Parameters  $A, B, C$  have been received by fitting the dependence to standing

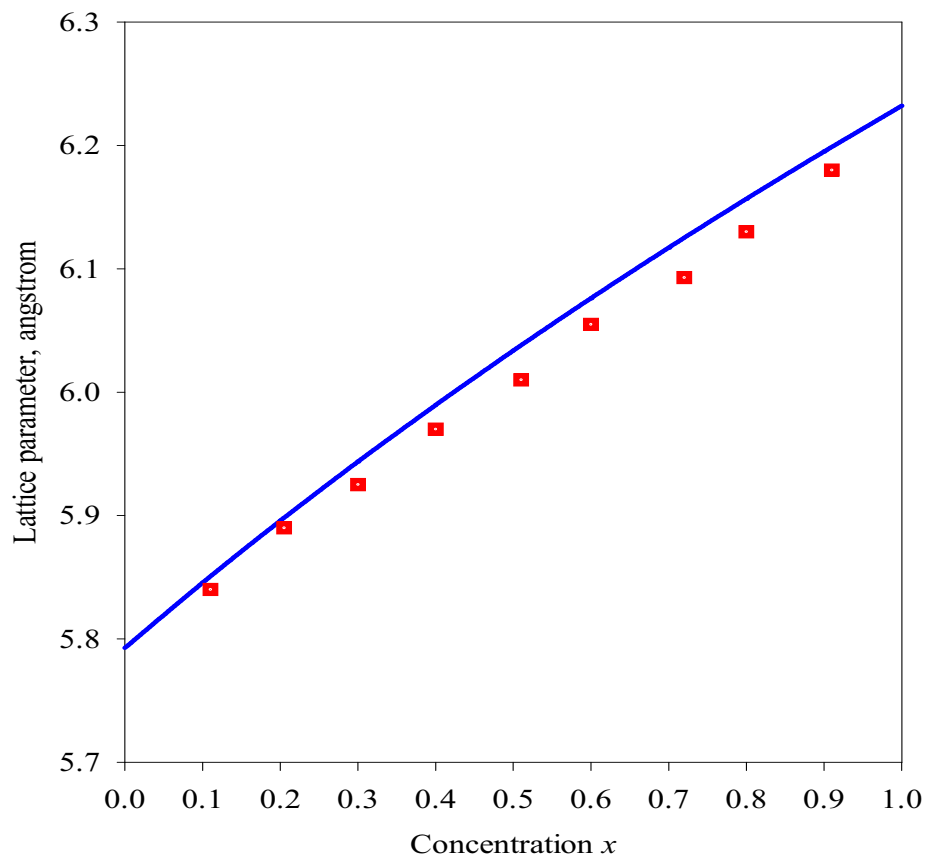


Figure 1: The lattice constant of  $Sr_{1-x}Ba_xF_2$  from  $x$ . Square symbol refer to experiment [1].

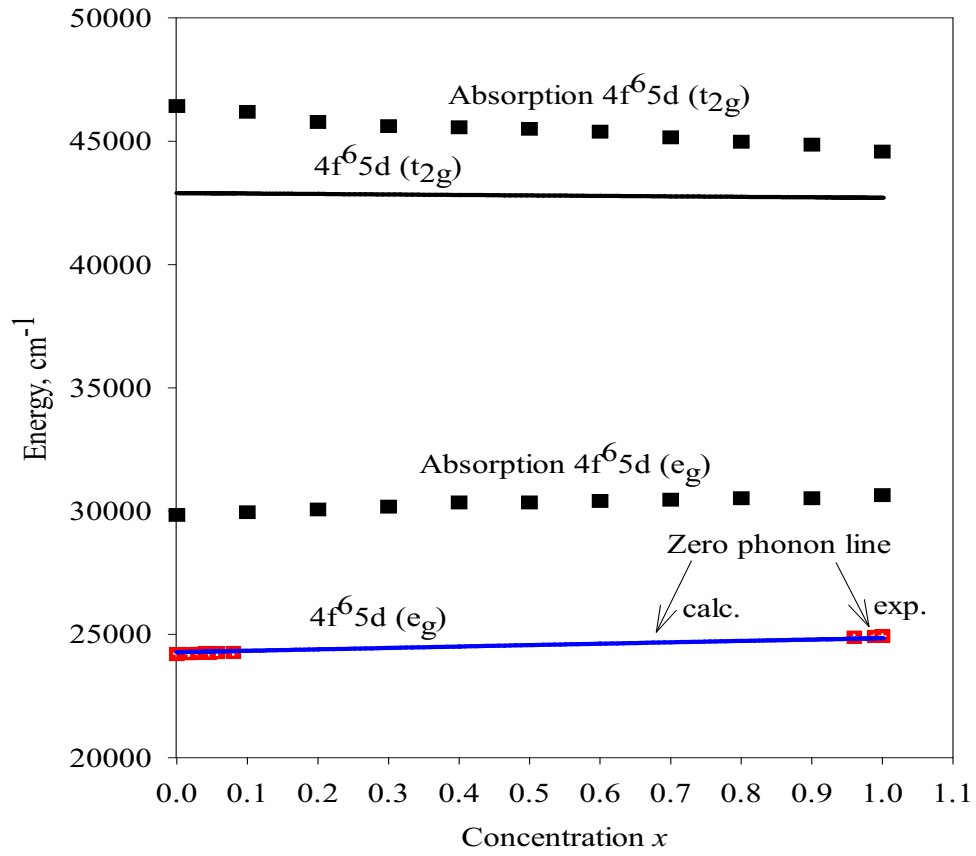


Figure 2:  $t_{2g}$  and  $e_g$  levels of  $\text{Eu}^{2+}$ . Square symbol refer to experiment[2].

ZPL in  $CaF_2$  and  $SrF_2$  crystals [2] and  $t_{2g} - e_g$  splitting in  $MeF_2$  ( $Me = Ca, Sr, Ba$ ) [3, 4]. The parameters are:  $A = 439,7 \times 10^6 cm^{-1} \times \text{\AA}^{12}$ ,  $B = 280 \times 10^5 cm^{-1} \times \text{\AA}^5$ ,  $C = 36940 cm^{-1}$ . The dependence of ZPL position from  $x$  we can receive using calculated distance  $Eu^{2+} - F^-$  in  $Ca_{1-x}Sr_xF_2 : Eu^{2+}$  at various  $x$ . It is possible to calculate the  $t_{2g}$ -level position by means of [7] taking into account that third term in [7] is equal to  $6Dq$  (fig.2). The difference of the calculated  $t_{2g}$ -level position with short-wave adsorption peak can be explained by Stokes shift in adsorption.

The blue and yellow luminescence is observed in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$  for  $x \in [0.2, 0.5]$  in intervals 430 – 450 and 500 – 580 nm. accordingly. The yellow luminescence at  $x > 0.5$  is only observed [3]. Yellow luminescence due to interconfigurational transitions between levels of impurity exciton (which is formed by transition of electron to twelve nearby cations) and the ground state  $^8S(4f^7)$  [3, 10] (fig.3). Position of  $e_g$ -level can be calculated in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$  using the expression (1). The top of valence band is formed by  $2p$ -states of fluorine in  $SrF_2$  and  $BaF_2$ . The bottom of conduction band is formed by  $s$ -states of cation. Forbidden zone varies practically linearly in row  $CaF_2$ ,  $SrF_2$ ,  $BaF_2$  [9]. The distance from  $e_g$  level to bottom of conduction band in  $SrF_2 : Eu^{2+}$  was taken from McClure work [10]. Assuming the position of  $2p$ -states of fluorine does not change at replacing cations  $Sr^{2+}$  by  $Ba^{2+}$ , it is possible to calculate the changing of conduction zone bottom as a function from  $x$ . According to ours calculation,  $e_g$ -level will be in a conduction band for  $x = 0.2$  in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$ . The yellow luminescence will begin at this  $x$  in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$  [3]. We have calculated configuration curves connected with  $A_{1g}$ -coordinate knowing how the energy of the crystal  $E$  depends on compression or expansion of a fluorine cube which surrounds  $Eu_{2+}$ . The deduced dependences  $E(Q)$  (where  $Q$ -is the symmetrical coordinate) for  $Sr_{1-x}Ba_xF_2 : Eu_{2+}$  are close to parabolic form  $kQ^2/2$ . Similar calculations was carried out for exciton state. The coefficient  $k$  dependences of the configurational curves on  $x$  are received:  $k_{ES} = 33.95 - 5.26 * x$ ,  $k_{GS} = 21.18 - 4.61 * x$ , where  $x \in [0, 1]$ , ( in  $eV \times \text{\AA}^{-2}$ ). The coefficients  $k_{ES}$  and  $k_{GS}$  are decreasing at increasing the barium concentration. It compounded with the fact that the elastic modules  $BaF_2$  are less than  $SrF_2$ . The fluorine cube is exposed to compression at formation of the exciton, the compression depends linearly on the concentration  $x$  in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$ :  $\Delta R = 0.143 + 0.036 * x$  (in  $\text{\AA}$ ). We can receive the Stokes shift for yellow luminescence as we know  $k_{GS}$  and change of distance  $Eu^{2+} - F^-$  at transition from exciton to the ground state:

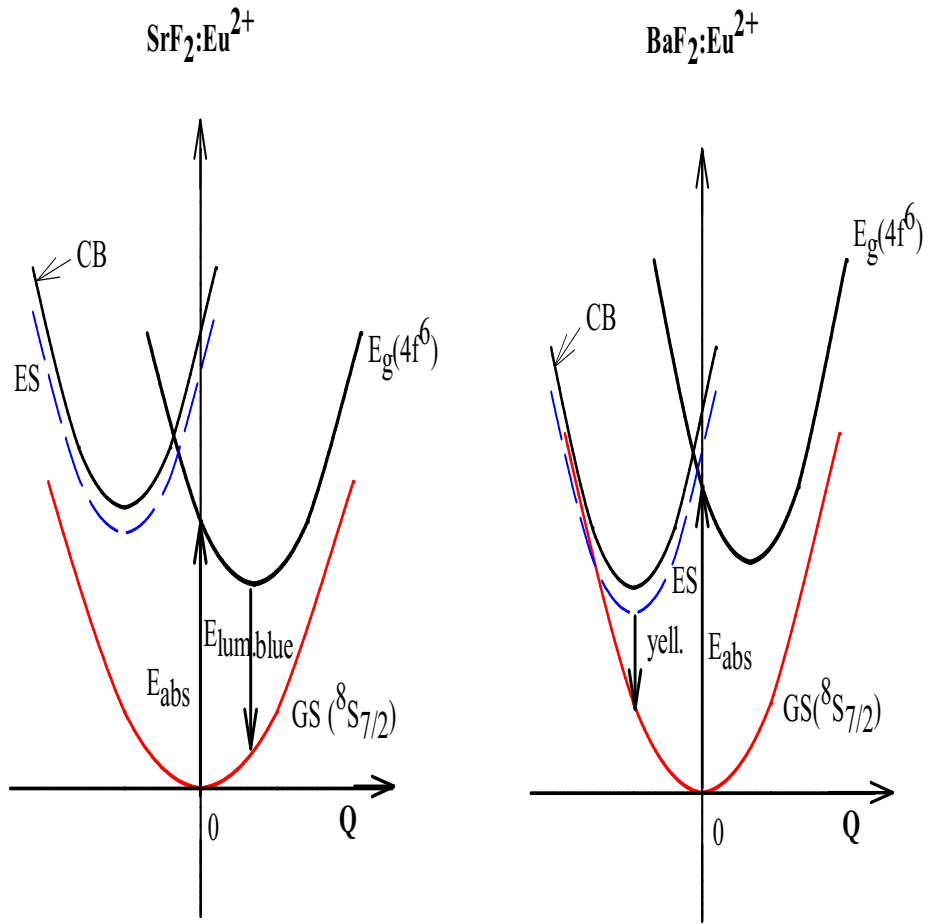


Figure 3: Configuration coordinate diagrams for describing of the blue and yellow luminescence in  $\text{CaF}_2 : \text{Eu}^{2+}$  and  $\text{SrF}_2 : \text{Eu}^{2+}$  [10]

$E_s = 1090 * x + 5011$  (in  $cm^{-1}$ ). The yellow luminescence have been observed in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$  at  $x \in [0.2, 1]$ , and with increasing  $x$  its peak is shifting to the long-wave part of the spectrum [3]. According to our calculation the Stokes shift is increased on  $800cm^{-1}$ . We can estimate  $A_{1g}$  frequency of a cube from eight ions  $F^-$ :

$$\nu_{A_{1g}} = \sqrt{\frac{k_{GS}}{m_F}} \quad (2)$$

where  $m_F$  – a mass of the fluorine. According to our calculations  $n = 547 - 63 * x$ , ( $n$  in  $cm^{-1}$ ). We can calculate Huang-Rhys factor for yellow luminescence as we know  $E_s$  and  $n$ . The factor is increasing from 9 to 12 at increasing  $x$  from 0 to 1 in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$ .

## 4 Conclusion

The method of virtual crystal implemented in shell model and framework of pair potential approximation allows us to calculate the crystal structure and lattice constant for mixed fluorites  $Ca_{1-x}Sr_xF_2$  and  $Sr_{1-x}Ba_xF_2$ . This method allows us to calculate the distance  $Eu^{2+} - F^-$  in doped crystals  $Ca_{1-x}Sr_xF_2 : Eu^{2+}$  and  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$ . The low level position of excited  $4f^65d$  configuration of an ion  $Eu^{2+}$  is expressed by phenomenological dependence on  $Eu^{2+} - F^-$  distance. The dependences of Stokes shift and Huang-Rhys factor on  $x$  have been calculated for yellow luminescence in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$ . According to our calculation the Stokes shift is increasing by  $1000cm^{-1}$ , the Huang-Rhys factor is increasing from 9 to 12 while  $x$  changes from 0 to 1. According to calculation the  $e_g$  level of  $Eu^{2+}$  ion will be within the conduction band for  $x \geq 0.2$  in  $Sr_{1-x}Ba_xF_2 : Eu^{2+}$ .

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